

ROMANIAN MATHEMATICAL MAGAZINE

If $a, b > 0$, $a + b = 2$ then:

$$\frac{a}{\sqrt{2-a}} + \frac{b}{\sqrt{2-b}} \geq 2$$

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Solution by Tapas Das-India

$$\begin{aligned} \frac{a}{\sqrt{2-a}} + \frac{b}{\sqrt{2-b}} &= \frac{a^{\frac{3}{2}}}{\sqrt{2a-a^2}} + \frac{b^{\frac{3}{2}}}{\sqrt{2b-b^2}} \stackrel{\text{Radon}}{\geq} \\ &\geq \frac{(a+b)^{\frac{3}{2}}}{\sqrt{2(a+b)-(a^2+b^2)}} \stackrel{\text{CBS}}{\geq} \frac{(a+b)^{\frac{3}{2}}}{\sqrt{2(a+b)-\frac{(a+b)^2}{2}}} \stackrel{a+b=2}{=} \frac{2^{\frac{3}{2}}}{\sqrt{4-2}} = 2 \end{aligned}$$

Equality holds for $a = b = 1$