

ROMANIAN MATHEMATICAL MAGAZINE

$\lambda \in \mathbb{R}$ fixed. Solve for reals :

$$3^{x+\lambda} + 3x + 3\lambda = 1$$

Proposed by Marin Chirciu-Romania

Solution by Tapas Das-India

$$\text{Let } y = x + \lambda$$

The equation can be written as $3^y + 3(y - \lambda) + 3\lambda = 1$ or, $3^y + 3y = 1$ (1)

*Let $f(y) = 3^y + 3y$ then $f'(y) = 3^y \ln 3 + 3 > 0 \forall y \in \mathbb{R}$
 $f(x)$ is strictly increasing*

For this equation (1) has at most one solution, clearly $f(0) = 1$

$y = 0$ satisfy the equation (1)

$y = 0$ is a solution or $x + \lambda = 0$ or $x = -\lambda$