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$$\Omega = \int \left(\frac{\sinh^2 x}{\sinh(2x) - 2x} - \frac{x \cdot \sinh x}{\sinh x - x \cdot \cosh x} \right) dx$$

Proposed by Daniel Sitaru-Romania

Solution by Igor Soposki-Skopje-Macedonia

$$\begin{aligned} \Omega &= \int \left(\frac{\sinh^2 x}{\sinh(2x) - 2x} - \frac{x \cdot \sinh x}{\sinh x - x \cdot \cosh x} \right) dx = I_1 + I_2 \\ I_1 &= \int \frac{\sinh^2 x}{\sinh(2x) - 2x} dx = \int \frac{\sinh^2 x}{2 \sinh x \cdot \cosh x - 2x} dx = \\ &= \frac{1}{2} \int \frac{\sinh^2 x}{\sinh x \cdot \cosh x - x} dx \stackrel{\sinh x \cosh x - x = t}{=} \frac{1}{4} \int \frac{dt}{t} = \frac{1}{4} \log |\sinh(2x) - 2x| + C_1 \\ I_2 &= \int \frac{x \cdot \sinh x}{\sinh x - x \cdot \cosh x} dx \stackrel{\sinh x - x \cosh x = t}{=} - \int \frac{dt}{t} = -\log |\sinh x - x \cdot \cosh x| + C_2 \\ I &= \frac{1}{4} \log |\sinh(2x) - 2x| - \log |\sinh x - x \cdot \cosh x| + \end{aligned}$$

Note by editor:

Many thanks to Florică Anastase-Romania for typed solutions.